

1 次の式を因数分解せよ。

(1)  $xy^2 - 2xy$

(2)  $4x^2 - 4x + 1$

(3)  $9x^2 + 12xy + 4y^2$

(4)  $64x^2y^2 - 25$

(5)  $x^2 - 5x + 6$

(6)  $x^2 - 6x - 16$

(7)  $2x^2 - 3x - 5$

(8)  $6x^2 + x - 15$

(9)  $(x + 2y)^2 - 3(x + 2y) + 2$

(10)  $(2a - b)^2 + 7(2a - b)$

2 次の値を求めよ。

(1)  ${}_6C_3$       (2)  ${}_8C_4$       (3)  ${}_{10}C_0$       (4)  ${}_{10}C_9$       (5)  ${}_{100}C_{98}$

(6)  ${}_7C_3$       (7)  ${}_8C_3$       (8)  ${}_5C_1$       (9)  ${}_6C_6$

□ (1)  $xy^2 - 2xy = xy \times y - 2 \times xy = xy(y - 2)$

(2)  $4x^2 - 4x + 1 = (2x)^2 - 2 \times 2x \times 1 + 1^2 = (2x - 1)^2$

(3)  $9x^2 + 12xy + 4y^2 = (3x)^2 + 2 \times 3x \times 2y + (2y)^2 = (3x + 2y)^2$

(4)  $64x^2y^2 - 25 = (8xy)^2 - 5^2 = (8xy + 5)(8xy - 5)$

(5) 和が-5, 積が6となるのは-2と3より、

$$x^2 - 5x + 6 = (x - 2)(x - 3)$$

(6) 和が-6, 積が-16となるのは-8と2であるから

$$x^2 - 6x - 16 = (x - 8)(x + 2)$$

(7) 積が2, 積が-5となることから

$$2x^2 - 3x - 5 = (x + 1)(2x - 5)$$

$$\begin{array}{r} 2 \quad -5 \\ \hline 1 \quad +1 \longrightarrow +2 \\ 2 \quad -5 \longrightarrow -5 \\ \hline -3 \end{array}$$

(8) 積が6, 積が-15となることから

$$6x^2 + x - 15 = (2x - 3)(3x + 5)$$

$$\begin{array}{r} 6 \quad -15 \\ \hline 2 \quad -3 \longrightarrow -9 \\ 3 \quad +5 \longrightarrow +10 \\ \hline +1 \end{array}$$

(9)  $x + 2y = A$  とおくと

$$\begin{aligned} & (x + 2y)^2 - 3(x + 2y) + 2 \\ &= A^2 - 3A + 2 \\ &= (A - 1)(A - 2) \\ &= (x + 2y - 1)(x + 2y - 2) \end{aligned}$$

(10)  $2a - b = A$  とおくと

$$\begin{aligned} & (2a - b)^2 + 7(2a - b) \\ &= A^2 + 7A = A(A + 7) \\ &= (2a - b)(2a - b + 7) \end{aligned}$$

□

(1)  ${}_6C_3 = \frac{6 \times 5 \times 4}{3 \times 2 \times 1} = 20$

(2)  ${}_8C_4 = \frac{8 \times 7 \times 6 \times 5}{4 \times 3 \times 2 \times 1} = 70$

(3)  ${}_{10}C_0 = 1$

(4)  ${}_{10}C_9 = {}_{10}C_{10-9} = {}_{10}C_1 = \frac{10}{1} = 10$

(5)  ${}_{100}C_{98} = {}_{100}C_{100-98} = {}_{100}C_2 = \frac{100 \times 99}{2 \times 1} = 4950$

(6)  ${}_7C_3 = \frac{7 \times 6 \times 5}{3 \times 2 \times 1} = 35$

(7)  ${}_8C_3 = \frac{8 \times 7 \times 6}{3 \times 2 \times 1} = 56$

(8)  ${}_5C_1 = \frac{5}{1} = 5$

(9)  ${}_6C_6 = {}_6C_{6-6} = {}_6C_0 = 1$

(別解)  ${}_6C_6 = \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{6 \times 5 \times 4 \times 3 \times 2 \times 1} = 1$